

$f(t)$

**Real
Fourier series**

$$f(t) = a_0 + \sum_{n=1}^{\infty} \left[a_n \cos\left(\frac{n\pi t}{p}\right) + b_n \sin\left(\frac{n\pi t}{p}\right) \right]$$

$$a_0 = \frac{1}{2p} \int_{-p}^p f(t) dt$$

$$a_n = \frac{1}{p} \int_{-p}^p f(t) \cos\left(\frac{n\pi t}{p}\right) dt, \quad n=1, 2, 3, \dots$$

$$b_n = \frac{1}{p} \int_{-p}^p f(t) \sin\left(\frac{n\pi t}{p}\right) dt, \quad n=1, 2, 3, \dots$$

**Complex
Fourier series**

$$f(t) = \sum_{n=-\infty}^{\infty} c_n e^{i \frac{n\pi t}{p}}$$

$$c_n = \frac{1}{2p} \int_{-p}^p f(t) e^{-i \frac{n\pi t}{p}} dt$$

Fourier 轉換

$t \leftrightarrow \omega$

$F(\omega)$

**Fourier Integral
(Fourier 正轉換)**

$$F(\omega) = \int_{-\infty}^{\infty} f(t) e^{-i\omega t} dt$$

Fourier 逆轉換

$$f(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} F(\omega) e^{i\omega t} d\omega$$

$i\omega \leftrightarrow s$

$F(s)$

Laplace 正轉換

$$F(s) = \int_0^{\infty} f(t) e^{-st} dt$$

Laplace 逆轉換

$$f(t) = \frac{1}{2\pi i} \int_{\alpha-i\infty}^{\alpha+i\infty} F(s) e^{st} ds$$

Laplace 轉換

$t \leftrightarrow s$