

國立臺灣海洋大學河海工程學系1997 工程數學 (三) 第九次作業

1. In the course, we have solved the particular solution (steady state solution) of the SDOF vibration system

$$\ddot{x} + x = \cos(3t)$$

$$\ddot{x} + x = \sin(3t)$$

- (1). conventional method.
 - (2). method of complex variables.
 - (3). Discuss the change of amplitude and phase between input and output and plot it in complex plane.
- (Hint: by superimposing real and imaginary part)

2. Solve the particular solution (steady state solution) of the SDOF vibration system

$$\ddot{x} + \dot{x} + x = \cos(3t)$$

$$\ddot{x} + \dot{x} + x = \sin(3t)$$

- (1). conventional method.
 - (2). method of complex variables.
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3. Solve the particular solution (steady state solution) of the SDOF vibration system

$$\ddot{x} + \dot{x} + x = \cos(3t)$$

$$\ddot{x} + \dot{x} + x = \sin(3t)$$

- (1). check the phase of $x_p(t) = a \cos(3t) + b \sin(3t) = c \cos(3t + \phi)$
- (2). check the phase of $x_p(t) = p \cos(3t) + q \sin(3t) = r \sin(3t + \psi)$
- (3). check the phase of $z = R e^{i\theta} e^{i\omega t}$
- (4). What is the relation of c, r and R ?
- (5). What is the relation of ϕ, ψ and θ ?