

### Meshless formulation for plate vibration



$$\nabla^4 u(x) = \mathbf{I}^4 u(x), \quad x \in D$$

$$u(x) = 0, \quad x \in B$$

$$\text{where } \mathbf{I}^4 = \frac{\mathbf{W}^2 \mathbf{R} h}{k}, \quad k = \frac{Eh^3}{12(1-\mathbf{n}^2)}$$

#### 1. Circular case

Analytical study using circulants  
SVD updating techniques  
True and Spurious eigenvalues  
Numerical experiment

#### 2. Square case

Numerical experiment

$$U(s, x) = \text{Im}\{U_c(s, x)\}, \quad (1) \quad U_c(s, x) = -\frac{i}{8\mathbf{I}^2} \{H_0^{(1)}(\mathbf{I}r) - H_0^{(1)}(i\mathbf{I}r)\} \quad (\text{Kitahara})$$

$$3. \quad (2) \quad U_c(s, x) = \text{Re}\{-\frac{i}{8\mathbf{I}^2} \{H_0^{(1)}(\mathbf{I}r) - H_0^{(1)}(i\mathbf{I}r)\}\} \quad (\text{Hutchinson})$$

$$(3) \quad U_c(s, x) = AJ_0(kr) + BI_0(kr) \quad (\text{Kang})$$

#### 4. Meshless formulation

#### 5. Determination of eigenvalues and eigenmodes

#### 6. Exact solution:

$$J_n(\mathbf{I})I_{n+1}(\mathbf{I}) + I_n(\mathbf{I})J_{n+1}(\mathbf{I}) = 0, \quad \text{for clamped circular plate}$$