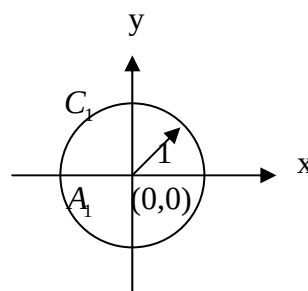


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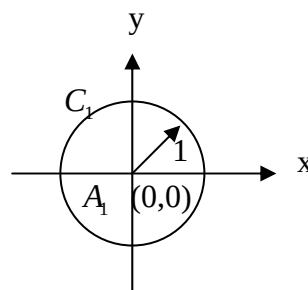
$$1. \oint_C \left(\frac{-y}{x^2 + y^2} \right) dx + \left(\frac{x}{x^2 + y^2} \right) dy = ?$$

where C_1 and A_1 are shown below.



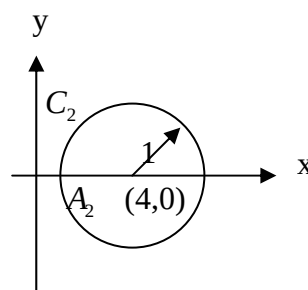
$$2. \iint_A \left[\frac{\partial}{\partial x} \left(\frac{x}{x^2 + y^2} \right) - \frac{\partial}{\partial y} \left(\frac{-y}{x^2 + y^2} \right) \right] dA = ?$$

where C_1 and A_1 are shown below.



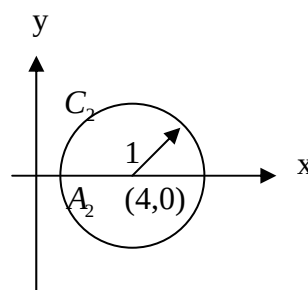
$$3. \oint_C \left(\frac{-y}{x^2 + y^2} \right) dx + \left(\frac{x}{x^2 + y^2} \right) dy = ?$$

where C_2 and A_2 are shown below.



$$4. \iint_A \left[\frac{\partial}{\partial x} \left(\frac{x}{x^2 + y^2} \right) - \frac{\partial}{\partial y} \left(\frac{-y}{x^2 + y^2} \right) \right] dA = ?$$

where C_2 and A_2 are shown below.



5. Green theorem is ok or not?